



# Assignment

## Properties of Logarithms

### Basic Level

1.  $\log ab - \log |b| =$   
(a)  $\log a$       (b)  $\log |a|$       (c)  $-\log a$       (d) None of these
2. The value of  $\sqrt{(\log_{0.5}^2 4)}$  is  
(a) -2      (b)  $\sqrt{(-4)}$       (c) 2      (d) None of these
3. The value of  $\log_3 4 \log_4 5 \log_5 6 \log_6 7 \log_7 8 \log_8 9$  is  
(a) 1      (b) 2      (c) 3      (d) 4      [IIT Allahabad 2000]
4.  $\log_7 \log_7 \sqrt{7(\sqrt{7\sqrt{7}})} =$   
(a)  $3 \log_2 7$       (b)  $1 - 3 \log_3 7$       (c)  $1 - 3 \log_7 2$       (d) None of these
5. The value of  $81^{(1/\log_5 3)} + 27^{\log_9 36} + 3^{4/\log_7 9}$  is equal to  
(a) 49      (b) 625      (c) 216      (d) 890
6.  $7 \log\left(\frac{16}{15}\right) + 5 \log\left(\frac{25}{24}\right) + 3 \log\left(\frac{81}{80}\right)$  is equal to  
(a) 0      (b) 1      (c)  $\log 2$       (d)  $\log 3$       [EAMCET 1990]
7. If  $\log_4 5 = a$  and  $\log_5 6 = b$ , then  $\log_3 2$  is equal to  
(a)  $\frac{1}{2a+1}$       (b)  $\frac{1}{2b+1}$       (c)  $2ab+1$       (d)  $\frac{1}{2ab-1}$
8. If  $\log_k x \cdot \log_5 k = \log_x 5, k \neq 1, k > 0$ , then  $x$  is equal to  
(a)  $k$       (b)  $\frac{1}{5}$       (c) 5      (d) None of these
9. If  $\log_5 a \cdot \log_a x = 2$ , then  $x$  is equal to  
(a) 125      (b)  $a^2$       (c) 25      (d) None of these
10. If  $a^2 + 4b^2 = 12ab$ , then  $\log(a+2b)$  is  
(a)  $\frac{1}{2}[\log a + \log b - \log 2]$       (b)  $\log \frac{a}{2} + \log \frac{b}{2} + \log 2$       (c)  $\frac{1}{2}[\log a + \log b + 4 \log 2]$       (d)  $\frac{1}{2}[\log a - \log b + 4 \log 2]$
11. If  $A = \log_2 \log_2 \log_4 256 + 2 \log_{\sqrt{2}} 2$ , then  $A$  is equal to  
(a) 2      (b) 3      (c) 5      (d) 7      [WB JEE 1992]
12. If  $\log_{10} x = y$ , then  $\log_{1000} x^2$  is equal to  
(a)  $y^2$       (b)  $2y$       (c)  $\frac{3y}{2}$       (d)  $\frac{2y}{3}$

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13. If  $x = \log_a(bc), y = \log_b(ca), z = \log_c(ab)$ , then which of the following is equal to 1  
(a)  $x+y+z$       (b)  $(1+x)^{-1} + (1+y)^{-1} + (1+z)^{-1}$       (c)  $xyz$       (d) None of these
14. If  $a = \log_{24} 12, b = \log_{36} 24$  and  $c = \log_{48} 36$ , then  $1+abc$  is equal to  
(a)  $2ab$       (b)  $2ac$       (c)  $2bc$       (d) 0
15. If  $a^x = b, b^y = c, c^z = a$ , then value of  $xyz$  is  
(a) 0      (b) 1      (c) 2      (d) 3
16. If  $\log x : \log y : \log z = (y-z):(z-x):(x-y)$  then  
(a)  $x^y \cdot y^z \cdot z^x = 1$       (b)  $x^x y^y z^z = 1$       (c)  $\sqrt[x]{x} \sqrt[y]{y} \sqrt[z]{z} = 1$       (d) None of these
17.  $\log_4 2 - \log_8 2 + \log_{16} 2 - \dots$  to  $\infty$  is [MNR 1994; Roorkee 1994; MP PET 2000]  
(a)  $e^2$       (b)  $\ln 2 + 1$       (c)  $\ln 2 - 1$       (d)  $1 - \ln 2$
18. If  $\log_{10} 2 = 0.30103, \log_{10} 3 = 0.47712$ , the number of digits in  $3^{12} \times 2^8$  is  
(a) 7      (b) 8      (c) 9      (d) 10
19.  $\sum_{r=1}^{89} \log_3(\tan r^\circ)$   
(a) 3      (b) 1      (c) 2      (d) 0
20.  $\sum_{n=1}^{\infty} \frac{1}{\log_{2^n}(a)} =$   
(a)  $\frac{n(n+1)}{2} \log_a 2$       (b)  $\frac{n(n+1)}{2} \log_2 a$       (c)  $\frac{(n+1)^2 n^2}{4} \log_2 a$       (d) None of these
21. Which of the following is not true  
(a)  $\log(1+x) < x$  for  $x > 0$       (b)  $\frac{x}{1+x} < \log(1+x)$  for  $x > 0$       (c)  $e^x > 1+x$  for  $x > 0$       (d)  $e^x < 1-x$  for  $x > 0$
22. The solution of the equation  $\log_7 \log_5(\sqrt{x^2 + 5 + x}) = 0$  [UPSEAT 2000 (S.E.)]  
(a)  $x = 2$       (b)  $x = 3$       (c)  $x = 4$       (d)  $x = -2$

**Advance**

23.  $\log_4 18$  is  
(a) A rational number      (b) An irrational number      (c) A prime number      (d) None of these
24. The value of  $(0.05)^{\log \sqrt{20}(0.1+0.01+0.001+\dots)}$  is  
(a) 81      (b)  $\frac{1}{81}$       (c) 20      (d)  $\frac{1}{20}$
25. If  $a, b, c$  are distinct positive numbers, each different from 1, such that  $[\log_b a \log_c a - \log_a a] + [\log_a b \log_c b - \log_b b] + [\log_a c \log_b c - \log_c c] = 0$ , then  $abc =$

- |       |       |       |                   |
|-------|-------|-------|-------------------|
| (a) 1 | (b) 2 | (c) 3 | (d) None of these |
|-------|-------|-------|-------------------|
- 26.** If  $\log_{12} 27 = a$ , then  $\log_6 16 =$  [EAMCET 1990]
- |                               |                               |                               |                   |
|-------------------------------|-------------------------------|-------------------------------|-------------------|
| (a) $2 \cdot \frac{3-a}{3+a}$ | (b) $3 \cdot \frac{3-a}{3+a}$ | (c) $4 \cdot \frac{3-a}{3+a}$ | (d) None of these |
|-------------------------------|-------------------------------|-------------------------------|-------------------|
- 27.** If  $n = 1983!$ , then the value of expression  $\frac{1}{\log_2 n} + \frac{1}{\log_3 n} + \frac{1}{\log_4 n} + \dots + \frac{1}{\log_{1983} n}$  is equal to
- |        |       |       |       |
|--------|-------|-------|-------|
| (a) -1 | (b) 0 | (c) 1 | (d) 2 |
|--------|-------|-------|-------|
- 28.** If  $\frac{\log x}{b-c} = \frac{\log y}{c-a} = \frac{\log z}{a-b}$ , then which of the following is true
- |               |                       |                                   |                         |
|---------------|-----------------------|-----------------------------------|-------------------------|
| (a) $xyz = 1$ | (b) $x^a y^b z^c = 1$ | (c) $x^{b+c} y^{c+a} z^{a+b} = 1$ | (d) $xyz = x^a y^b z^c$ |
|---------------|-----------------------|-----------------------------------|-------------------------|
- 29.** If  $x_n > x_{n-1} > \dots > x_2 > x_1 > 1$  then the value of  $\log_{x_1} \log_{x_2} \log_{x_3} \dots \log_{x_n} x_n^{x_{n-1} \dots x_1}$  is equal to
- |       |       |       |                   |
|-------|-------|-------|-------------------|
| (a) 0 | (b) 1 | (c) 2 | (d) None of these |
|-------|-------|-------|-------------------|
- 30.** The number of solution of  $\log_2(x+5) = 6 - x$  is
- |       |       |       |                   |
|-------|-------|-------|-------------------|
| (a) 2 | (b) 0 | (c) 3 | (d) None of these |
|-------|-------|-------|-------------------|
- 31.** The number of real values of the parameter  $k$  for which  $(\log_{16} x)^2 - \log_{16} x + \log_{16} k = 0$  with real coefficients will have exactly one solution is
- |       |       |       |                   |
|-------|-------|-------|-------------------|
| (a) 2 | (b) 1 | (c) 4 | (d) None of these |
|-------|-------|-------|-------------------|
- 32.** If  $x^{\frac{3}{4}(\log_3 x)^2 + \log_3 x - \frac{5}{4}} = \sqrt{3}$  then  $x$  has
- |                                  |     |                      |
|----------------------------------|-----|----------------------|
| (a) One positive integral value  | (b) | One irrational value |
| (c) Two positive rational values | (d) | None of these        |

### Logarithmic Inequalities

#### Basic Level

- 33.** If  $x = \log_5(1000)$  and  $y = \log_7(2058)$  then
- |             |             |             |                   |
|-------------|-------------|-------------|-------------------|
| (a) $x > y$ | (b) $x < y$ | (c) $x = y$ | (d) None of these |
|-------------|-------------|-------------|-------------------|
- 34.** The number  $\log_{20} 3$  lies in
- |                                             |                                             |                                             |                                             |
|---------------------------------------------|---------------------------------------------|---------------------------------------------|---------------------------------------------|
| (a) $\left(\frac{1}{4}, \frac{1}{3}\right)$ | (b) $\left(\frac{1}{3}, \frac{1}{2}\right)$ | (c) $\left(\frac{1}{2}, \frac{3}{4}\right)$ | (d) $\left(\frac{3}{4}, \frac{4}{5}\right)$ |
|---------------------------------------------|---------------------------------------------|---------------------------------------------|---------------------------------------------|
- 35.** If  $\frac{1}{\log_3 \pi} + \frac{1}{\log_4 \pi} > x$ , then  $x$  be
- |       |       |         |           |
|-------|-------|---------|-----------|
| (a) 2 | (b) 3 | (c) 3.5 | (d) $\pi$ |
|-------|-------|---------|-----------|
- 36.** If  $\log_{1/\sqrt{2}} \sin x > 0$ ,  $x \in [0, 4\pi]$ , then the number of values of  $x$  which are integral multiples of  $\frac{\pi}{4}$ , is
- |       |        |       |                   |
|-------|--------|-------|-------------------|
| (a) 4 | (b) 12 | (c) 3 | (d) None of these |
|-------|--------|-------|-------------------|
- 37.** The set of real values of  $x$  satisfying  $\log_{1/2}(x^2 - 6x + 12) \geq -2$  is
- |                    |              |                    |                   |
|--------------------|--------------|--------------------|-------------------|
| (a) $(-\infty, 2]$ | (b) $[2, 4]$ | (c) $[4, +\infty)$ | (d) None of these |
|--------------------|--------------|--------------------|-------------------|
- 38.** The set of real values of  $x$  for which  $2^{\log_{\sqrt{2}}(x-1)} > x + 5$  is

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- (a)  $(-\infty, -1) \cup (4, +\infty)$       (b)  $(4, +\infty)$       (c)  $(-1, 4)$       (d) None of these

**Advance**

39. Solution set of inequality  $\log_{10}(x^2 - 2x - 2) \leq 0$  is

- (a)  $[-1, 1 - \sqrt{3}]$       (b)  $[1 + \sqrt{3}, 3]$       (c)  $[-1, 1 - \sqrt{3}) \cup (1 + \sqrt{3}, 3]$       (d) None of these

40. If  $\frac{1}{2} \leq \log_{0.1} x \leq 2$  then.....

- (a) The maximum value of  $x$  is  $\frac{1}{\sqrt{10}}$       (b)  $x$  lies between  $\frac{1}{100}$  and  $\frac{1}{\sqrt{10}}$

- (c)  $x$  does not lie between  $\frac{1}{100}$  and  $\frac{1}{\sqrt{10}}$       (d) The minimum value of  $x$  is  $\frac{1}{100}$

41. If  $\log_{0.04}(x-1) \geq \log_{0.2}(x-1)$  then  $x$  belongs to the interval

- (a)  $(1, 2]$       (b)  $(-\infty, 2]$       (c)  $[2, +\infty)$       (d) None of these

42. The set of real values of  $x$  for which  $\log_{0.2} \frac{x+2}{x} \leq 1$  is

- (a)  $\left(-\infty, -\frac{5}{2}\right] \cup (0, +\infty)$       (b)  $\left[\frac{5}{2}, +\infty\right)$       (c)  $(-\infty, -2) \cup (0, +\infty)$       (d) None of these

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